Quantifying early aftershock activity of the 2004 mid-Niigata Prefecture earthquake ($M_{w}$6.6)

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We analyze the early aftershock activity of the 2004 mid-Niigata earthquake, using both earthquake catalog data and continuous waveform recordings. The frequency-magnitude distribution analysis of the Japan Meteorological Agency (JMA) catalog shows that the magnitude of completeness of the aftershocks changes from values around 5.0, immediately after the main shock, to about 1.8, 12 hours later. Such a large incompleteness of early events can bias significantly the estimation of aftershock rates. To better determine the temporal pattern of aftershocks in the first minutes after the Niigata earthquake, we analyze the continuous seismograms recorded at six High Sensitivity Seismograph Network (Hi-Net) stations located close to the aftershock distribution. Clear aftershocks can be seen from about 35 s after the main shock. We estimate that the events we picked on the waveforms recorded at two seismic stations (NGOH and YNTH) situated on opposite sides of the aftershock distribution are complete above a threshold magnitude of 3.4. The $c$ value determined by taking these events into account is about 0.003 days (4.3 min). Statistical tests demonstrate that a small, but nonzero, $c$ value is a reliable result. We also analyze the decay with time of the moment release rates of the aftershocks in the JMA catalog, since these rates should be much less influenced by the missing small events. The moment rates follow a power law time dependence from few minutes to months after the main shock. We finally show that the rate-and-state dependent friction law or stress corrosion could explain well our findings.


1. Introduction

[2] The occurrence rate of aftershocks is empirically well described by the modified Omori law [Utsu, 1961]:

\[ n(t) = \frac{k}{(t + c)^p}, \]

where $n(t)$ is the frequency of aftershocks per unit time, at time $t$ after the main shock, and $k$, $c$, and $p$ are constants. The parameter $p$ indicates how fast the rate of aftershocks decays with time and has a value close to 1.0, regardless of the cutoff magnitude. The parameter $k$ is dependent on the total number of events in the sequence. The parameter $c$, which relates to the rate of aftershock activity in the earliest part of an aftershock sequence, typically ranges from 0.5 to 20 hours in empirical studies [Utsu et al., 1995]. Because of deficiencies in recording capabilities, an increased number of smaller early aftershocks are usually missing from seismic catalogs. Kagan [2004] shows that the incompleteness of aftershock data immediately after large main shocks is associated with a systematic bias of the $c$ parameter toward larger values and proposes that $c$ is essentially zero. Other researchers, however, argue that carefully checked catalog data may provide clues on physically based, nonzero $c$ values [e.g., Narteau et al., 2002; Shcherbakov et al., 2004; K. Z. Nanjo et al., The decay of aftershock activity for Japanese earthquakes, submitted to Journal of Geophysical Research, 2006]. Recent work [Vidale et al., 2003; Peng et al., 2006, 2007] brings clear evidence on the increased incompleteness of catalog data immediately after moderate to large earthquakes, while arguing for a deficiency of early aftershocks based on the analysis of high-quality waveform data. As these studies demonstrate, it is essential to accurately determine the $c$ value since the behavior of aftershock sequences during the first minutes and hours after the main shock is a significant component of theoretical models of seismicity [e.g., Dieterich, 1994; Gomberg, 2001; Rubin, 2002]. There is also recent interest in applying stochastic models of earthquake occurrence, employing a power law temporal aftershock decay, to evaluate the time-dependent earthquake probability, as discussed by Kagan [2004]. Therefore, knowing the characteristics of the early part of earthquake sequences is important for obtaining unbiased results.

[3] We focus in this study on the decay of the early aftershock activity following the 2004 mid-Niigata (Chuetsu) earthquake and try to estimate the $c$ parameter by using the Japan Meteorological Agency (JMA) earthquake...
2. Temporal Pattern of Early Aftershocks

2.1. JMA Catalog Data

[4] The map in Figure 1 displays the epicentral distribution of aftershocks (JMA data) for 134 days from the main shock, for $M \geq -0.2$. We chose for analysis all the earthquakes that cluster on and around the fault system in the Chuetsu aftershock region, with depths from 0 to 27 km [Shibutani et al., 2005]. Few small events, located significantly further from the aftershock cluster in Figure 1, were not included. We also considered a squared aftershock area centered on the mid-Niigata earthquake, with a size defined using the formula of Kagan [2002a] based on the magnitude of the main shock. The obtained data set was essentially the same with the one used in our analysis. The quality of the catalog is high due to the good station coverage in the area, which includes several Hi-Net stations. The main shock (JMA magnitude of 6.8; $M_{s}6.6$) had four large aftershocks with magnitudes of 6.3, 6.0, 6.5 and 6.1, which occurred 7 min, 16 min, 38 min, and 88 hours, respectively, after the main shock.

[5] We first analyze the frequency-magnitude distribution of the aftershocks using the JMA catalog with the standard relation of Gutenberg and Richter [1944]:

$$\log_{10} N = a - bM$$

where $N$ is the cumulative number of events having magnitude larger than and equal to $M$, and $a$ and $b$ are constants. Figures 2a, 2b, 2c, and 2d show the frequency-magnitude distribution of earthquakes 0.01, 0.05, 0.2, and 0.5 day, respectively after the main shock, for 100-event windows. We assume that the deviation of the data from a power law fit for small magnitudes is due to the incomplete detection of smaller events. Following a similar procedure to that of Wiemer and Wyss [2000], we determine the magnitude of completeness ($Mc$) as the magnitude at which 95% of the data can be modeled by a power law fit. The $Mc$ value, estimated using the cumulative frequency-magnitude distribution, is also checked against the noncumulative version of the Gutenberg-Richter law. The $b$ value in each case is obtained using a maximum likelihood procedure [Aki, 1965; Utsu, 1969], considering only the earthquakes with magnitudes $M \geq Mc$. As Figure 2 clearly shows, $Mc$ decreases with time from the main shock. This is consistent with the assumption that there is an improvement with time of the recording capability of small earthquakes. The $b$ values for Figures 2b to 2d are 0.8, which are typical values for aftershock sequences [Utsu, 1969]. In Figure 2a, the $b$ value is slightly larger (0.87), but the estimation accuracy might be lower since there are only about 20 events, with magnitudes above $Mc$, used for the fit.

[6] Figure 3 shows the magnitude versus time from the main shock for the aftershocks of the JMA catalog. It is clearly seen that as the time from the main shock increases, progressively smaller earthquakes are recorded in the catalog. Thus aftershocks with $M \geq 4.0$, $M \geq 3.0$ and $M \geq 2.0$ become completely recorded from about 23, 114, and 216 min, respectively, from the main shock. We also plot in Figure 3 the $Mc$ values, as determined from the frequency-magnitude distributions (Figure 2). These points fit well (coefficient of determination is 0.99) a least squares regression line with

$$Mc(t) = 1.5 - 1.4 \log_{10} (t)$$

where $Mc(t)$ is the magnitude of completeness at time $t$ after the main shock. Equation (3) describes the catalog completeness versus time, down to a magnitude of about 1.8. In Figure 3 we plot, for comparison, an average magnitude of completeness line for southern California aftershocks, as determined from equation (15) of Helmstetter et al. [2006] for main shocks with magnitudes $M = 6.6$. As can be seen, at very early times after the main shock, even moderate size aftershocks ($M \sim 4.5$) can be missing from the catalog. This is in agreement with Kagan and Houston [2005], who show that it is very difficult to accurately estimate the $c$ value by analyzing standard catalog data.

2.2. Hi-Net Waveform Data

[7] As pointed out in section 2.1, there are probably many small earthquakes missing from the catalog data immediately after the main shock. Therefore we try to detect as many early events as possible on vertical component velocity seismograms recorded at Hi-Net borehole stations (Figure 1) situated close to the aftershock distribution. Because of the large amplitudes of the main shock coda waves, it is difficult to accurately identify early aftershocks...
on the original recordings. Thus, to identify the high-frequency signals from the aftershocks, we high-pass-filtered the waveforms. Similar techniques have been used to separate tectonic events from volcanic tremor at times of high volcanic seismicity [e.g., Qamar et al., 1983] or to reveal nuclear tests “hidden” in natural earthquakes [e.g., Sykes, 1986]. We tried several cutoff frequencies: 7, 15, 20, and 25 Hz. Figure 4 shows the results obtained by applying a 7 Hz high-pass Butterworth filter to the continuous seismograms of six stations. The amplitudes were normalized by the largest value. One can identify clear early aftershocks on the filtered waveforms, starting about 35 s after the main shock. The results are similar when using higher cutoff frequencies and, in few cases, smaller magnitude events are easier to identify. However, the high-frequency noise is also amplified for higher cutoffs, and this hinders the correct picking of events. Therefore we decided to continue our analysis using the 7 Hz high-pass-filtered seismograms.

We selected two Hi-Net stations (NGOH and YNTH), situated on opposite sides of the aftershock distribution, and counted the events with maximum amplitudes above some threshold value, which can be clearly identified on the waveforms. For the NGOH station we used about 40 min of continuous data. Unfortunately, station YNTH functioned well for only 5 min after the main shock, so we used the data recorded during this shorter period of time. In several cases, when we were not sure about an event identified at one of the two stations, we also checked the filtered seismograms recorded at the other four stations. For the identified events we cannot determine precisely their absolute occurrence time. However, since both NGOH and YNTH stations are close to the aftershock region, we approximate their occurrence time with the arrival time, which should be accurate to within a few seconds. To avoid counting both the \( P \) and \( S \) arrivals from the same event, we checked all picks visually. We finally obtained two data sets of 423 and 65 picks at NGOH and YNTH stations, respectively.

We plot in Figure 5 the cumulative number of picked events at station NGOH versus the logarithm of their relative, maximum amplitude, measured on rescaled seismograms. For amplitudes above some threshold value the data can be well fit by a straight line with a slope of 1.18 and a standard deviation of 0.03. In analogy with the frequency-magnitude distribution, the amplitudes that fit the linear relation reflect the completeness level of our picked events. Comparing with located events in the

![Figure 2. Frequency-magnitude distribution of aftershocks (a) 0.01 day, (b) 0.05 day, (c) 0.2 day and (d) 0.5 day after the main shock, for 100-event windows. The cumulative and noncumulative numbers of earthquakes are shown by rectangles and triangles, respectively. The solid lines represent maximum likelihood fits to the data for magnitudes above the magnitude of completeness, \( Mc \). The \( Mc \), \( a \), and \( b \) values for each case are also shown.](image-url)
JMA catalog, we find that we are able to identify earthquakes with magnitudes $M \geq 3.4$, which occurred later than about 35 s after the main shock. There were 41 aftershocks with $M \geq 3.4$ recorded in the JMA catalog in the first 40 min after the main shock and all of them had relative amplitudes above the 0.028 amplitude threshold. Comparing the amplitudes in our data with the JMA magnitudes for these events, we estimate an uncertainty of about ±0.1 for our magnitude determinations. We noticed, however, that the amplitudes of the largest events picked on the filtered waveforms start to saturate for magnitudes larger than about 4.5. Such a saturation may explain why the slope (1.18 ± 0.03) of the linear fit in Figure 5 is larger than the $b$ values (≈0.8) determined previously from the JMA catalog data. The saturation of the larger amplitudes means there is an underestimate of the number of large events (and thus an increase of the slope’s value). A similar analysis was performed for the YNTH station, where we could also identify events above a threshold magnitude of 3.4. Most of the events above this threshold, picked at NGOH and YNTH stations, were also successfully identified on the continuous seismograms of other Hi-Net stations. We note that the Niigata aftershocks were relatively deep; thus there is probably no significant bias due to locations of events close to the stations.

Figure 3 shows the decay of the Niigata aftershock rates using the numbers of events picked at stations NGOH and YNTH, combined with the JMA data for later times. We selected only aftershocks with $M \geq 3.4$ to compute the logarithmically binned decay rates. The results of the

Figure 4. Vertical component velocity seismograms at six Hi-Net stations (see Figure 1), high-pass filtered at 7 Hz and normalized to the maximum amplitude observed on all seismograms. The names of the recording stations and the corresponding distances to the Niigata main shock are shown. The origin time corresponds to the main shock $P$ wave arrival at YNTH station (1756:3.5 LT, Japanese time). The occurrence time of the main shock is 1756:0.3 LT. The arrows indicate early aftershocks detected on seismograms after filtering.
analysis show a $c$ value of 0.003 days (4.32 min). For comparison, the $c$ value determined using only the JMA catalog has a much larger value of 0.017 days (24.48 min) because of the incompleteness of the data.

[11] The results presented in Figure 6 indicate that the $c$ value of the modified Omori law is relatively small, on the order of just a few minutes. We estimate that the aftershock data sets obtained by picking events on the filtered seismograms are complete for events larger than 3.4 (Figure 5), and that the $c$ value is not a result of incomplete detection of early aftershocks. To help verify our results, we also check how many events we are “missing” that leads to this $c$ value.

[12] The number of aftershocks, $N$, predicted by the modified Omori law (equation (1)) in a certain time interval ($t_1 < t < t_2$) after the main shock can be easily estimated as

$$N(t_1, t_2) = \int_{t_1}^{t_2} n(t) dt = \int_{t_1}^{t_2} \frac{k}{(t+c)^p} dt$$

where $n(t)$ is the aftershock rate and $k, c$ and $p$ are the modified Omori law’s parameters. We also know that an aftershock sequence can be described statistically as a nonstationary Poisson process, with the modified Omori law (equation (1)) as intensity function [Ogata, 1983].

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**Figure 5.** “Frequency-magnitude” like distribution, showing the cumulative number of picked events at NGOH station versus the logarithm of their relative, maximum amplitude, measured on rescaled seismograms. $Mc$ marks the relative amplitude above which our picked event data is complete and corresponds to a magnitude of about 3.4. Because of the high-pass filtering of the waveforms, the magnitudes estimated from the relative amplitudes start saturating around $M = 4.5$. The fit of the data above $Mc$ has a slope of 1.18, with a standard deviation of 0.03.

**Figure 6.** Aftershocks decay rate with time for the JMA catalog data (pluses) and for the events picked on the waveform data at NGOH (circles) and YNTH (crosses) stations. Only events with $M \geq 3.4$ are used. Data were logarithmically binned. The dashed line represents the modified Omori law (equation (1)) fit of the JMA catalog data (287 events) and has the following parameters: $p = 1.1 \pm 0.04$, $c = 0.017 \pm 0.006$, and $k = 33.05 \pm 2.61$. The solid line represents the modified Omori fit for the combined data of JMA catalog and NGOH station aftershocks (for the overlapping part we used the last source). The fit has the following parameters: $p = 1.13 \pm 0.02$, $c = 0.003 \pm 0.001$, and $k = 33.83 \pm 2.01$. The solid and dotted arrows in the upper part of the figure indicate the $c$ values for the combined data and the JMA data, respectively.
Then, the probability $P(x)$ of exactly $x$ events occurring in the time range $(t_1 \leq t < t_2)$ is [Cinlar, 1975]

$$P(x) = \left[ \int_{t_1}^{t_2} n(t) \, dt \right]^x \exp \left( -\int_{t_1}^{t_2} n(t) \, dt \right) / x! \quad (5)$$

where $n(t)$ is the intensity function (in our case, the aftershocks rate).

[13] We consider $t_1 = 35$ s, since we consider that we could count aftershocks which occurred later than about 35 s from the main shock. We take $t_2 = 220$ s, which is slightly smaller than the $P$ wave arrival time of a larger aftershock (M5.3) at the two seismic stations. We also take $p = 1.13$ and $k = 33.83$ as for the modified Omori fit in Figure 6 but assume that $c = 0$. Using formula (4), the number of aftershocks predicted to occur between 35 s and 220 s, from the main shock, is 156. We show in Figure 7 the continuous seismogram recorded at NGOH station for a time period of 220 s from the occurrence of the main shock. The red arrows mark the arrival times of events with absolute amplitude values larger than 0.028. The ±0.028 thresholds are indicated by horizontal gray lines. The pluses on the abscissa indicate 35 s after the main shock.

The events picked on the continuous waveforms may have some estimation uncertainties. However, the observations of the non–power law decay for the rates of the early aftershocks are similar at two stations situated on different
for each earthquake in the JMA catalog, Kagan and Houston [1990], which,

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sides of the earthquake distribution (NGOH and YNTH), suggesting that our results are reliable. We conclude that for

the analyzed seismic c value is small, but has a nonzero value on the order of a few minutes. This result agrees well with a c value of 130 s obtained by Peng et al. [2006] for the aftershocks of the 2004 M 6.0 Parkfield, California, earthquake, by analyzing waveform data from near-source seismometers.

As pointed out by Helmstetter et al. [2005], one of the problems with estimating aftershock properties is the difficulty in distinguishing between the “direct” (triggered by the main shock only) and “secondary” aftershocks (triggered by a previous aftershock). One may address such an issue only by using a stochastic model like ETAS [e.g., Ogata, 1989]. The fits of the aftershocks decay in Figure 6 did not account for the secondary aftershocks separately. However, the data fit a modified Omori law well and therefore the determined p, c and k parameters characterize well the temporal decay of this aftershock sequence. The occurrence of M 6.3 and M 6.0 aftershocks after 7 min (0.005 days) and 16 min (0.026 days) from the main shock, respectively, probably extended the time periods for which smaller aftershocks are not completely reported in the catalog. This, in turn, makes the determination of the real c values even more difficult. We also note that strong secondary aftershock sequences may produce “bumps” in aftershocks decay rates or the p value estimated from the fit of formula (1) to the data may become large. This is not the case, however, with the Niigata sequence. The p values we determined for several threshold magnitudes are around 1.1, a value similar to the average p values reported in the literature [Utsu et al., 1995; Reasenberg and Jones, 1989]. It was reported [Toda and Kondo, 2005] that the Niigata sequence exhibits a larger number of moderate- to-large aftershocks than other similar aftershock sequences.

This translates into relatively higher k values for the modified Omori fit of the Niigata aftershocks decay.

3. Moment Release of Aftershocks

[18] The difficulty of estimating real c values from the decay of aftershock rates in seismic catalogs led Kagan and Houston [2005] to an alternative approach. They study the moment release rate of aftershocks as a function of time, which has the advantage that the small events missing in the catalog have much less effect because their seismic moments are relatively small. However, the summation of seismic moments carries a significant price: random fluctuations of the sum are large, because of the small number of

summands [Zaliapin et al., 2005; Kagan and Houston, 2005].

[19] From the formula of Takemura [1990], which relates the JMA magnitude, M, with the seismic moment

$$Mo(N*m):$$

$$\log Mo = 1.17M + 10.72$$

we calculated Mo for each earthquake in the JMA catalog, except the four largest aftershocks of the sequence ($M \geq 6.0$). For these large events, we used the moments determined by NIED from waveforms inversion.

[20] Assuming that the aftershock size distribution follows the Gutenberg-Richter relation, one can also calculate the moment rate which is due to the missing small aftershocks. To compensate for an incomplete catalog record, we applied a multiplicative correction coefficient to the raw, total seismic moment in an aftershock time interval. The coefficient (C), given by equation (7) of Kagan and Houston [2005], depends on the lower moment threshold,

$$M_{sp},$$

of the aftershock sequence and the maximum moment

$$M_{sp}:$$

$$C = 1 - (\frac{M_{sp}}{M_{sp}})^{1-\beta}$$

where $\beta = 2b/3$ [Kagan, 2002b] and b is the b value of the frequency-magnitude distribution.

[21] The threshold moment ($M_a$) is computed using equations (3) and (6), while $M_{sp}$ is taken as the moment magnitude of the largest aftershock in a certain time period after the main shock, as in the study of Kagan and Houston [2005]. As alternative possibilities, we also equated $M_{sp}$ with the moment of the main shock or to the moment magnitude of the largest aftershock in the sequence. No significant differences between the results were found. We considered $b = 0.8$. The results of the moment rate decay are shown in Figure 8.

[22] In Figure 8, there is little difference between the overall moment release rate calculated using the catalog data and the corrected rates, which account for the under-reported small aftershocks. However, there is a difference at the very beginning of the aftershock sequence (first time interval). Figure 8 suggests that the aftershock moment rate can be approximated by a modified Omori law time dependence:

$$Mr(t) = k'(t + c')^p,$$
Mr and $r$ is dimensionless and is determined from the combined value of the aftershocks. The corrected $k$ is characteristic values (around $1/C_0 = c_c$). $c_A$ is background earthquake rate, $c_c$ values obtained from aftershock [Ben-Zion and Lyakhovsky, 2004; Dieterich, 1994], as it has been widely used to explain the temporal pattern of aftershocks.

$$R(t, \tau) = \frac{r}{(e^{(\Delta \tau/A \sigma)} - 1)e^{-t/\tau} + 1}$$  \hspace{1cm} (9)$$

where $r$ is background earthquake rate, $A$ is dimensionless fault constitutive parameter; $\sigma$ is normal stress; $\Delta \tau$ is shear stress step due to the main shock and $t_\sigma$ is characteristic relaxation time for the perturbation of earthquake rate (aftershock duration). The aftershock duration, $t_\sigma$, is:

$$t_\sigma = \frac{A \sigma}{\tau}$$  \hspace{1cm} (10)$$

where $\tau$ is the stressing rate, assumed to be the same before and after the main shock. Equation (9) has the following form:

$$n(t) = k''/(t + c'')$$  \hspace{1cm} (11)$$

with $k''$ and $c''$ values given by

$$k'' = (A \sigma/\tau)r$$  \hspace{1cm} (12)$$

$$c'' = (A \sigma/\tau) \exp\left(\frac{-\Delta \tau}{A \sigma}\right)$$  \hspace{1cm} (13)$$

Equation (11) is a particular case of the modified Omori law (equation (1)) for $p = 1$. If $p = 1$, $k'' = k$ and $c'' = c$, of the modified Omori law. If $p$ is not equal to one, which is the case of the Niigata sequence, the values are slightly different.

In the case of Niigata earthquake, we estimated the background rate, $r$, by analyzing the seismicity from 1994 to the occurrence time of the 2004 Niigata earthquake, in the aftershock area of the large event. We obtained $r = 0.0052$ events/d. This result agrees well with the background rates reported by Toda and Kondo [2005] for several cutoff magnitudes.

Figure 9 shows the decay of aftershock activity of the Niigata earthquake obtained by combining the JMA catalog data with the NGOH station data for the early aftershocks. Only events with $M \geq 3.4$ are used for computing the rates (same as in Figure 6). We use a nonlinear regression technique to fit these data with equation (10), which has two unknown parameters, $t_\sigma$ and $\Delta \tau/A \sigma$. The best fit obtained from the inversion is shown as a solid line in Figure 9 and is characterized by $t_\sigma = 5553.75$ days ($\sim 15$ years) and $\Delta \tau/A \sigma = 15.59$. The coefficient of multiple determination

4. Discussion

The underlying physics of the temporal decay of aftershocks has attracted much attention from seismologists. Many mechanisms have been proposed, e.g., postseismic creep [e.g., Benioff, 1951], fluid diffusion [Nur and Booker, 1972], rate-and-state dependent friction [Dieterich, 1994], stress corrosion [Yamashita and Knopoff, 1987; Gomberg, 2001] and damage mechanics [Main, 2000; Shcherbakov and Turcotte, 2004; Ben-Zion and Lyakhovsky, 2006]. We focus in this study on the rate-and-state dependent model [Dieterich, 1994], as it has been widely used to explain the temporal pattern of aftershocks.
for the fit is 0.98, which indicates that Dieterich's model fits the data well. We also show the fit of the aftershock rates by the modified Omori law (equation (1)). The values of the parameters $p$, $c$, and $k$ are those indicated for the solid line fit in Figure 6. For most of the data the Dieterich model and the modified Omori law fit the data well.

[30] As mentioned previously, the fit by equation (9) implies a $p$ value of 1.0 for the aftershocks decay. The fit by the modified Omori law, however, shows that the earthquake rates decay slightly faster ($p = 1.1$). This faster decay indicates that the background seismicity level, $r$, will be reached faster and therefore $t_0$ would be smaller than predicted by Dieterich's model. Also, the $c$ value estimated by use of equation (13) is 0.001, smaller than predicted by the modified Omori law. The only way to account for $p > 1$ in the rate-and-state model is to assume that the stress $\tau$ decreases with the logarithm of time after the main shock. However, the number of unknown parameters of the model is larger in such a case, so it becomes more difficult to invert for all of them from the aftershock data (the problem becomes less well constrained).

[31] The $\Delta t$ values in the crust are associated with a large range of values. Toda et al. [1998], for example, estimated $\Delta t = 0.35$ bars, from the study of aftershocks of the 1995 Kobe earthquake. Assuming this value and the result $\Delta t/\Delta t = 15.59$, we obtain a stress change $\Delta\tau$ of 5.45 bars. Such a value may be understood as an average over the aftershock region, which includes high values of $\Delta\tau$ close to the main shock rupture and the much smaller values at farther distances from the fault [Miyaizawa et al., 2005].

[32] In their review paper, Kanamori and Brodsky [2004] showed that the stress corrosion mechanism [e.g., Das and Scholz, 1981; Gomberg, 2001] predicts a similar behavior for the aftershock decay rates as the rate-and-state dependent friction law, with differences in the long-term return to the background level. In particular, the early aftershock rates deviate from a power law time decay ($\sim 1/t$). We also tested this model for the Niigata sequence and obtained a similar fit as for the rate-and-state dependent friction model.

[33] The delayed onset of the power law temporal decay of aftershocks may also be an effect of other phenomena, like strong ground shaking, episodic aseismic slip, healing or fluid diffusion [Vidale et al., 2003; Peng et al., 2007]. Further detailed analysis of high-quality data is necessary to test the predictions of various models and better understand the aftershock generation process.

5. Conclusions

[34] The magnitude of completeness of the aftershocks in the JMA catalog changes from values around 5.0, immediately after the Niigata main shock, to about 1.8, 12 hours later. This significant variation mainly reflects the gradual improvement with time of the recording capabilities of smaller earthquakes. The incompleteness of smaller aftershocks in the early part of the sequence introduces a bias in the estimation of the $c$ value. If one uses data where small events are missing, a probably better approach to obtain quick information about the early part of an aftershock sequence is to study the decay of the moment release rate of aftershocks. The delay time $\tau$ inferred using this technique is 0.0046 days (6.6 min) for the “original” moment rates (i.e., without any correction).

[35] In order to get more information on the aftershocks in the early part of the Niigata sequence, we analyzed the high-quality waveform data at six Hi-Net stations located close to the aftershock distribution. We counted events on high-pass-filtered waveforms starting from about 35 s after the main shock. The picked aftershocks are complete above a threshold amplitude that corresponds to a JMA magnitude of 3.4. By analyzing these data together with the JMA catalog of aftershocks, we estimated that the $c$ value is $0.003 \pm 0.001$ days (4.3 min).

[36] Statistical testing shows that the rates of aftershocks in the first few minutes of the sequence deviate significantly from a power law decay and the rate-and-state dependent friction law or stress corrosion may provide a good physical explanation.

[37] Acknowledgments. We thank NIED and JMA for allowing us to use their earthquake data. B.E. is grateful to the Japan Society for the Promotion of Science (JSPS) for providing him a postdoctoral scholarship to do research at DPRI, Kyoto University. We acknowledge very useful discussions with Hiroo Kanamori and David Jackson. We benefited from the thoughtful comments of the Editor, John C. Mutter, the anonymous Associate Editor and the two reviewers, Zhigang Peng and Ian Main.

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